The Effects on Cardiovascular Autonomic Control of Repetitive Arousal from Sleep

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Study Objectives: To quantitatively assess autonomic cardiovascular control in normal young adults following exposure to repetitive acoustically-induced arousals from sleep.

Design: Respiration, R-R interval (RRI) and noninvasive measurements of continuous arterial blood pressure were monitored in subjects during the transition from relaxed wakefulness to stable Stage 2 sleep. These measurements were made under undisturbed conditions or conditions in which transient arousals were induced repetitively by acoustic stimulation. A mathematical model was used to partition the fluctuations in RRI into a component (“RSA”) correlated with respiration and a component (“ABR”) representing baroreflex control of heart rate. The magnitudes and forms of each component before and after exposure to repetitive arousals were compared.

Setting: Sleep disorders laboratory in a university setting.

Patients or Participants: Ten healthy young adults (5 male, 5 female) with an average age of 20.4 ± 2.0 y and mean body-mass index of 23.8 ± 2.9 kg/m².

Interventions: Each subject participated in multiple sleep studies consisting of 4 conditions with 2 nights in each condition. The first condition consisted of undisturbed sleep (control), while in the other 3 conditions, the subjects were aroused from sleep by repetitive auditory stimuli applied continuously over a duration of 50 minutes, with periodicities of 30 seconds, 1 minute, and 2 minutes of sleep.

Measurements and Results: Exposure to repetitive arousal (RA) did not alter mean heart rate or blood pressure. However, ABR and RSA gains estimated using the model, increased from the onset of Stage 1 sleep to the start of stable Stage 2 sleep under the control condition, but remained unchanged in all RA conditions. There were also significant increases in low-frequency oscillations of systolic blood pressure in the RA conditions versus no change in the control condition.

Conclusions: Exposure to RA over durations approximating an hour produces cumulative effects on autonomic control that are subtle and can only be detected when advanced signal processing methods are employed. More specifically, the increases in ABR and RSA gains that accompany increasing sleep depth in normal sleep are prevented from occurring.

Keywords: Autonomic nervous system, cardiovascular control, mathematical model, respiratory sinus arrhythmia, baroreflexes

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INTRODUCTION

IT IS NOW REASONABLY WELL ESTABLISHED THAT OBSTRUCTIVE SLEEP APNEA (OSA) CONSTITUTES AN INDEPENDENT RISK FACTOR FOR DAYTIME HYPERTENSION.1,2 The potential mechanisms that could link OSA to hypertension include chronic exposure to intermittent hypoxia, large intrathoracic pressure swings, and repetitive arousals from sleep occurring at the termination of each obstructions.3 However, the extent to which each of these mechanisms contributes to the development of hypertension remains relatively unexplored, particularly in humans.

Previous studies have suggested a strong relationship between arousal from sleep and an increase in sympathetic nervous system activity and blood pressure (BP).4-6 In healthy subjects, the cardiovascular activation response at arousal from sleep is different from the response that occurs during normal wakefulness.7 In OSA, transient auditory arousal from sleep has been found to be associated with BP elevation even in the absence of apnea and hypoxia.8 Indeed, during NREM sleep in subjects with OSA, transient arousal alone causes much of the blood pressure rise at the end of each apnea.9 Thus, the question arises as to whether exposure to repeated transient arousals from sleep, in the absence of hypercapnia or hypoxia, produces cumulative effects on autonomic control.

Previous studies have shown that in normal individuals and in hypertensive subjects without sleep disordered breathing, NREM sleep is associated with a lowering of heart rate, arterial blood pressure, cardiac output, and systemic vascular resistance.10-12 These changes are consistent with the general notion that the parasympathetic branch of the autonomic nervous system assumes dominance during normal sleep. On the other hand, some studies indicate that this increase in parasympathetic activity and the corresponding decrease in sympathetic activity are not achieved monotonically. For instance, in one report, the magnitude of respiratory sinus arrhythmia (RSA) and total heart rate variability (HRV) were found to be increased in light sleep relative to wakefulness, but became lower in the deeper stages of NREM sleep.13 In a recent study in young healthy adults, Carrington et al.14 found that sleep was associated with an abrupt fall in BP, a small increase in the sensitivity of the baroreflex and, on the basis of indirect evidence, a downward resetting of the baroreflex. However, these effects were delayed by spontaneous arousals during the sleep onset period and were not manifest until stable sleep was achieved.14 In a study of normal, hypertensive,
Ten healthy volunteers (5 male, 5 female) were recruited; average age was 20.4 ± 2.0 y (range 18-25 y) and mean BMI of 23.8 ± 2.9 kg/m$^2$ (range 18.2-29.1 kg/m$^2$). Participants were screened via questionnaire at an intake interview for personal, familial, or medical conditions that could affect sleep quality. Volunteers were free of physical illness and were not, or had not been taking any medication other than birth control pills, although menstrual phase was not controlled for. Volunteers did not participate during times of major life stress, such as during examination periods. The project was approved by the Human Research Ethics Committee of The University of Melbourne. Lastly, participants gave informed consent to participate in the study and were reimbursed for their time commitment to the study.

In each subject, the electromyogram, electrooculogram, electroencephalogram, BP, electrocardiogram (ECG), and respiratory inductance plethysmograph (abdominal and thoracic) were recorded. BP was measured continuously and noninvasively using a Portapres Model 2 BP Monitor (TNO-TPD Biomedical Instrumentation, Amsterdam, The Netherlands).

**Experimental Design**

Each subject participated in multiple sleep studies consisting of 4 conditions with 2 nights in each condition. The first condition was normal sleep in which participants were left to sleep undisturbed. In the other 3 conditions, the subjects were aroused by repetitive auditory stimuli with periodicities of 30 s, 1 min, and 2 min of sleep. For each subject, the order in which the control and each of the repetitive arousal conditions were applied was randomized.

For each condition the data were classified into 5 phases corresponding to sleep status. Phase 1, 30 min prior to lights out (LO), corresponded to the initial period of relaxed wakefulness prior to the lights being turned out. Phase 2, LO to the onset of stage 1 sleep, was marked by relaxed wakefulness after LO and before the first occurrence of 10 s of continuous theta activity. Phase 3, onset of stage 1 sleep to the onset of stage 2 sleep, corresponded to the time between the first 10 s of continuous theta activity and the first sleep spindle or K-complex. Phase 4, onset of stage 2 sleep to the onset of stable stage 2 sleep, corresponded to the time between the first 10 s of continuous theta activity and the first sleep spindle or K-complex. Phase 5, onset of stable stage 2 sleep, corresponded to the time between the first occurrence of a sleep spindle or K-complex and the beginning of stable stage 2 sleep, as defined by the beginning of the first 5 min of undisturbed NREM sleep. Phase 5, 30 min after onset of stage 2 sleep, was marked by undisturbed sleep as characterized by continuous stage 2 sleep or slow wave sleep (SWS) without arousal. In conditions 2, 3, and 4, in which repetitive auditory stimuli were presented, stable NREM sleep did not occur. Thus, phase 4 was defined as having the same duration as Phase 4 in condition 1, and Phase 5 was defined as the next 30 minutes. A schematic summary of the experimental protocol is displayed in Figure 1.

**Data Analysis**

R-R intervals (RRI) were extracted from the ECG. Systolic blood pressure (SBP) and diastolic blood pressure (DBP) were

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**Figure 1**—Schematic summary of the experimental protocol showing the duration over which repetitive arousals were elicited acoustically (box marked “50 min”), as well as the approximate time-locations of the data segments extracted for analysis (boxes with vertical bars).
extracted on a beat-by-beat basis. Instantaneous lung volume (V) was calculated from the abdominal and thoracic respiration bands signals. All signals were detrended and uniformly sampled to 2 samples/s. To eliminate high-frequency noise, the data were preprocessed by low-pass filtering using a Kaiser finite impulse response filter (pass- band = 0-0.5 Hz, stop band = 0.7-1 Hz, order 21, and ripple < 0.01).

Because of the incompleteness of some of the studies, and in order to maintain the same repetitive arousal periods for each subject, data from only 7 participants were processed. In order to eliminate first-night effects, only the data from the second night for each condition were analyzed. For each signal, 5 consecutive 30-s segments towards the end of phase 3 and 5 corresponding 30-s segments after 50 min of repetitive arousal (in phase 5) were selected for further analysis (see Figure 1).

From each segment of data, the following parameters were calculated: mean RRI, mean BP, low-frequency RRI power (RRI_{LFP}), ratio of low-frequency to high-frequency RRI power (RRI_{LFHFP}) and low-frequency SBP power. Subsequently, two-way repeated measures analysis of variance was applied to each of the above parameter estimates. The first factor was phase (pre-arousal in phase 3 vs post-arousal in phase 5). The second factor was repetitive arousal (RA) type, the levels being control (no arousal), 30 s RA, 1 min RA, and 2 min RA.

**Model**

To determine how changes in instantaneous lung volume (∆V) and fluctuations in SBP (∆SBP) dynamically produce fluctuations in RRI (∆RRI), we employed a mathematical model of heart rate variability based on that of Belozeroff et al., but modified to allow the model parameters to be time-varying. In this model (displayed schematically in Figure 2), fluctuations of RRI are autonomically mediated by the arterial baroreflexes (ABR) and direct respiratory-cardiac coupling (RSA), as represented by the equation below:

$$\Delta RRI(t) = \sum_{i=1}^{M} h_{RRI}(t-i) \cdot \Delta V(t-i - \tau_{RSA}) + \sum_{i=1}^{M} h_{SBP}(t-i) \cdot \Delta SBP(t-i - \tau_{ABR}) + \epsilon(t)$$

In the above equation, $h_{RRI}(\cdot)$ and $h_{SBP}(\cdot)$ represent the impulse responses that characterize the dynamics of the respiratory-cardiac coupling mechanism and the baroreflexes, respectively. $h_{ABR}(\cdot)$, quantifies the time-course of the change in RRI resulting from an abrupt increase in SBP of 1 mm Hg. $h_{RSA}(\cdot)$ reflects the time-course of the fluctuation in RRI following a very rapid inspiration and expiration of 1 liter of air. Note that the dependence on two time indices (t and i) implies that we are allowing $h_{RRI}(\cdot)$ and $h_{ABR}(\cdot)$ to represent dynamic characteristics that can vary with time. These impulse responses were assumed to persist for a maximum duration of M sampling intervals, each sampling interval being 0.5 s. Based on the lengths of our datasets and preliminary analyses, we found 50 to be a suitable value for M. Asyali has shown that the Meixner set provides better estimates of dynamic responses that contain pure delays. The practical advantage of this approach is that the use of basis functions produces a substantial reduction in the number of unknown parameters by an order of magnitude, thereby allowing greater statistical reliability to be achieved in the parameter estimates. Although we have previously employed Laguerre basis functions, Asyali has shown that the Meixner set provides better estimates of dynamic responses that contain pure delays. The first 2 minutes of data were used to obtain initial estimates of the Meixner coefficients. The “optimal” values of $\tau_{RRI}$, $\tau_{ABR}$, model order (number of Meixner functions) (4 to 8), and the order of the generalization (which controls when the family of Meixner functions begins to fluctuate), were obtained by selecting the combination...
of parameters that produced the smallest global values of the minimum description length (MDL) and the cross correlation between the residual error and input as criterion. Subsequently, the model was made time-varying by allowing the coefficients of the Meixner basis functions to change with time. The recursive least squares algorithm was used to estimate the time-varying coefficients of the model. Further details of the model calculations are given in the Appendix.

The estimation of the above impulse responses was improved by increasing the orthogonality between the 2 inputs. This was achieved by using an autoregressive model with exogenous input (ARX model) to “filter” out the respiration-correlated component of \( \Delta SBP \). Respiration and the respiration-uncorrelated \( \Delta SBP \) were then used as dual inputs to the model, as represented in Equation (1). Subsequently, the calculated \( h_{ARB}(\cdot) \) was kept unchanged while estimation of \( h_{RSA}(\cdot) \) was repeated using the respiration and original (unorthogonalized) blood pressure inputs.

From each impulse response function estimated at any time \( t \), the Fast Fourier Transform was computed to derive the transfer function at that time. Thus, the time-varying model allowed us to estimate the sequential estimates of the RSA and ABR transfer functions as time evolved from Phase 3 through Phase 5. For purposes of statistical analysis, the following descriptors were derived from each impulse response or transfer function estimate: 1) the peak to peak magnitude, which was the difference between the maximum and minimum value of the impulse response; 2) the “dynamic gain,” or the average transfer function magnitude between 0.04 and 0.4 Hz, which was obtained by computing the Fast Fourier Transform of the impulse response; 3) the high-frequency gain, the average transfer function magnitude between 0.15 and 0.4 Hz; and 4) the low-frequency gain, the average transfer function magnitude between 0.04 and 0.15 Hz. This procedure enabled us to generate the estimated time-courses of all model descriptors. To determine whether there were significant changes in the model descriptors before vs after the duration (50 min) of repetitive arousal, we selected for comparison the average of each model descriptor during the last 1-min segment of Phase 3 and the average of the same model descriptor during the first 1-min segment of Phase 5.

Two-way repeated measures analysis of variance was applied to each of the above estimated model descriptors. The first factor was Phase (pre-arousal in Phase 3 vs post-arousal in Phase 5). The second factor was repetitive arousal (RA) type, the levels being Control (no arousal), 30 s RA, 1 min RA, and 2 min RA. If differences occurred, post hoc pairwise comparisons were performed.

RESULTS

Effect of Repetitive Arousal on RRI, BP, and Cardiovascular Variability

Figure 3 displays examples of the changes in SBP elicited as a result of repeated arousals (indicated by dashed vertical bars) induced by acoustic stimulation at intervals of 30 s (top panel), 1 minute (middle panel), and 2 minutes (bottom panel). As shown in Table 1, none of the repetitive arousal regimens produced detectable cumulative effects on mean RRI, mean SBP and mean DBP. There was also no systematic effect of repetitive arousal on the spectral indices of heart rate variability, except for an increase in HFP要是 followed by 30 s RA and a decrease in LHR following 1-min RA. The potential reasons for these isolated changes are addressed in the Discussion.

However, there was a consistent increase in the low-frequency power of SBP variability (LFP_{SHP}) in all the arousal conditions between Phase 3 and Phase 5, whereas under control conditions LFP_{SHP} did not change. The low-frequency power of DBP variability (LFP_{DBP}) did not display the same tendency, except in the 30-s RA condition.

Effects of Repetitive Arousal on Model Parameters

The left panel of Figure 4 shows the estimated subject-averaged transfer functions (magnitude plots) for the RSA component of
the model in Phase 3 (filled circles) and Phase 5 (open triangles) in the control condition (i.e., natural sleep without interventions). The averaged Phase 1 plot is displayed for reference. The shapes of the estimated transfer functions suggest that the RSA mechanism behaves as a low-pass filter, i.e., as breathing frequency is decreased, the amplitude of the associated heart rate oscillation increases. This is consistent with the findings from previous studies that have investigated how RSA magnitude changes when breathing frequency is controlled voluntarily.19

On average, the RSA transfer function magnitude showed a tendency to be higher in Phase 5 relative to Phase 3. However, because of the high degree of variability in the data, this difference was only significant in the low-frequency range (see Table 2 and Figure 4). When the natural progression of sleep was interrupted through the repeated application of acoustic stimulation for 50 min, there was no increase in RSA transfer function magnitude between Phases 3 and 5 (Table 2). The left panel for Figure 4 displays the results for one of the repetitive arousal conditions (30-s RA).

The transfer function magnitude plots for the ABR component of the model for the control condition are shown in the left panel of Figure 5. Here, it is quite clear that the baroreflex transfer function increased in magnitude during the progression from Phase 3 to Phase 5, when there was uninterrupted sleep. In contrast, following 50 min of acoustically-induced arousals produced repeatedly every 30 s, the increase in ABR transfer

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Figure 3—Sample time-courses of the beat-to-beat fluctuations in systolic blood pressure (SBP) elicited as a result of repeated arousals (indicated by dashed vertical bars) induced by acoustic stimulation at intervals of 30 s (top panel), 1 min (middle panel), and 2 min (bottom panel).
DISCUSSION

Autonomic Effects of Obstructive Sleep Apnea: Intermittent Hypoxia vs Repetitive Arousal

Three major factors accompany each cycle of obstructive apnea: hypoxia, large changes in intrathoracic pressure, and transient arousal from sleep. Several recent studies involving animal models have provided useful insight into the relative importance of these individual factors in producing the chronic abnormalities of autonomic cardiovascular control associated with OSA. Using an elegant canine model of obstructive apnea, Brooks et al.21 were able to produce nocturnal and daytime hypertension by exposing the animals to artificially-induced periodic airway obstructions for several weeks. On the other hand, sustained exposure to periodic acoustically-induced arousals without prior upper airway obstruction led only to nocturnal hypertension with no carryover effect in the daytime. In a rat model, Fletcher et al.22,23 have shown that sustained hypertension develops after a
few weeks of exposure to intermittent hypoxia without any accompanying upper airway obstruction. In a porcine model, Chen and Scharf found the cardiovascular effects of simulated central apneas to be greater than those resulting from obstructive apneas of similar durations.24 These studies, taken together, suggest that although OSA is characterized by large intrathoracic pressure changes, episodic hypoxemia, and arousal-induced sleep fragmentation; hypoxic stimulation appears to be the dominant factor that produces the chronic alterations in autonomic cardiovascular control. On the other hand, the aforementioned studies were conducted on animal preparations. In humans, a retrospective study relating daytime plasma and urine norepinephrine levels to respiratory disturbance index, nocturnal arterial O₂ saturation and arousal index found an independent association between the measures of daytime sympathetic activity and movement arousals.12 In a recent study, 24-hour ambulatory blood pressure was monitored in 46 subjects with moderate-to-severe OSA before and after 2 weeks of either continuous positive airway pressure (CPAP) therapy or sham-CPAP with supplemental nocturnal oxygen.25 Following the treatment period, subjects treated with CPAP showed a significant reduction in daytime and nighttime blood pressures, whereas no changes were found in those subjects treated with sham-CPAP and supplemental nocturnal oxygen. This result suggests that elimination of intermittent hypoxia during the night per se did not have a major effect on cardiovascular autonomic control, and that the effectiveness of CPAP therapy was presumably due to the reduction in arousals and/or intrathoracic pressure changes. Thus, the relative contribution of repetitive arousal towards long-term impairment of cardiovascular control appears to differ between animals and humans.

Quantifying the Cumulative Effects of Arousal on Autonomic Control in Humans

The major finding of this study is that, although continuous exposure to repetitive arousals for a duration of approximately 1 hour does not produce any overt changes in mean heart rate or systolic or diastolic blood pressures, subtle changes in autonomic control can be detected through the application of a model-based approach to carefully examine the relationships linking respiration and SBP to heart rate variability. These cumulative effects are summarized in Figure 6. During unperturbed sleep onset, we found that baroreflex (ABR) gain increased with increasing depth of sleep. This was also the case with the RSA component, although the effect was substantially greater in the low-frequency region of the associated transfer function. However, ABR and RSA gains did not change significantly when sleep was interrupted by repetitive arousal. These findings suggest that the transition from Phase 3 to Phase 5 is accompanied by a reduction in sympathetic activity and/or increase in vagal tone, consistent with what has been reported in previous studies.10-15 Exposure to repetitive arousal appears to hinder this natural shift during sleep onset in sympathovagal balance towards greater vagal predominance and lower sympathetic tone. The periodicity with which the arousals are elicited appears to have no differential impact on their cumulative effect on autonomic control.

Another important observation from our study is that all 3 RA conditions led to an increase in the power of low-frequency oscillations in SBP in Phase 5. Increases in LFP₁ have been found to occur in association with conditions that increase sympathetic activation, such as head-up tilt, mental stress, and heart failure.26-28 Thus, our findings suggest that there was a gradual accumulation of the effects of sympathetic activation following each arousal, and that the progressive buildup of sympathetic tone offsets the tendency for sympathetic withdrawal that accompanies natural sleep onset.

Modeling Considerations

We have successfully employed the multivariate model displayed in Figure 2 to detect abnormalities in autonomic car-

Figure 5—Estimated subject-averaged transfer functions (magnitude plots) for the ABR component of the model in Phase 3 (filled circles) and Phase 5 (open triangles) in the control condition (left panel) compared to the corresponding cases for the 30-s RA condition. The subject-averaged Phase 1 plots are displayed for reference. Note that the tendency for ABR gain to increase from Phase 3 to Phase 5 in uninterrupted sleep does not occur following exposure to repetitive arousals.
diovascular control in OSA under a variety of conditions.\textsuperscript{16,29,30} The key strength of this approach is that it enables the partitioning of fluctuations in RRI (or equivalently, heart rate) into contributions that are associated directly with respiration and contributions that result from baroreflex buffering of fluctuations in BP. By relating these RRI components to their corresponding “inputs” (i.e., respiration and BP), the model allows the estimation of the underlying transfer functions (“RSA” and “ABR”). In doing so, we are able to circumvent some of the limitations inherent in other approaches (e.g., spectral analysis) that focus only on heart rate variability or blood pressure variability.\textsuperscript{27} Illustrative of the potential problems with employing spectral analysis of heart rate variability to quantify autonomic function are the isolated changes in HFP\textsubscript{RRI} and LHR following 30-s RA and 1-min RA, respectively, as reported in Table 1. Both of these conventional measures of heart rate variability do not take into account differences in respiration between Phase 3 and Phase 5. For instance, an increase in ventilation in Phase 5 relative to Phase 3 in some of the subjects would contribute to an increase in RRI spectral power in the high-frequency range, and thus lead to an increase in HFP\textsubscript{RRI} and decrease in LHR.

An important feature of our model-based approach is that our estimates of baroreflex gain are computed only after the component of the RRI fluctuations linearly correlated to respiration has been removed from RRI. In other methods that employ spontaneous blood pressure fluctuations for estimating baroreflex sensitivity, such as the “spectral” or “sequence”\textsuperscript{31} methods, the contribution of respiration to the fluctuations in RRI are not taken into consideration. A recent study has shown that excluding the effect of respiration on RRI can lead to the introduction of a significant amount of bias into the computation of baroreflex sensitivity.\textsuperscript{32}

Previous implementations of this model assumed stationarity in the data, thus requiring that our analyses be applied to data segments in which there were no obvious trends or apparent changes in dynamic behavior. We have recently extended the

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure6.png}
\caption{Comparison of the estimated average values for baroreflex gain (top panel) and low-frequency power of systolic blood pressure oscillations (LFP\textsubscript{SBP}) in Phase 3 vs Phase 5 under control, 30 s RA, 1 min RA, and 2 min RA conditions.}
\end{figure}
model to incorporate time-varying transfer functions. This allows us to bypass the stationarity assumption, and thus apply the model to situations in which ABR and/or RSA dynamics are suspected to be evolving with time, e.g., during and immediately following arousals. We have applied the time-varying model to this study, since our measurements were collected during a period in which a complex series of transitions were occurring: from quiet wakefulness immediately prior to the start of sleep onset to the time during which stable Stage 2 sleep was first identified. There are, however, differences in the details of the methodology between this version of the model and the model published by Blasi et al. These relate primarily to the use of Meixner basis functions in this study instead of the Laguerre set that we had previously employed. Meixner basis functions have been shown to produce improved parameter estimation results when the system under study contains significant time delays.

**Limitations of the Study**

To determine the cumulative effects of repetitive arousal on autonomic control, we induced transient arousals in normal subjects using acoustic stimulation. This differs from the usual mechanism for arousal in OSA, which is believed to involve the buildup of chemical drive and respiratory effort beyond specific thresholds prior to eliciting a response from the reticular activating system. Thus, in our study, some portion of the cardio-respiratory response to arousal could have originated from direct stimulation generated by the cochlear receptors. Moreover, by excluding the concurrent increases in chemical drive that accompany arousals in obstructive apneas, we have also ignored the possibility that arousal and hypoxia could have synergistic effects on autonomic function.

Another important limitation of this study is that the sequential arousals were carried out over a period of 50 minutes only. The effects on autonomic control were thus very small, as evidenced by the lack of any measurable changes in mean blood pressure or mean heart rate. Nevertheless, it is important to note that even this very minimalist intervention affected autonomic control. Future work should address the question of whether repetitive arousals applied over a longer total duration will amplify the small cumulative effects found in the present study. For instance, would cumulative exposure to repetitive arousal elicited over the entire sleep duration lead to measurable changes in morning cardiovascular autonomic function, as reflected in heart rate variability and blood pressure variability or even mean blood pressure? Furthermore, the current study was carried out on healthy young subjects. It would be important to determine the direction and magnitude of the cumulative autonomic effects produced by repetitive arousal in subjects with OSA or hypertensive subjects without OSA.

**CONCLUSIONS**

In summary, using spectral and model-based analyses of cardiovascular variability, we have found that exposure to repetitive acoustically-induced arousals over durations approximating an hour produces cumulative effects on autonomic control that are subtle and can only be detected when advanced signal processing methods are employed. More specifically, the increases in baroreflex and RSA gains that normally accompany increasing sleep depth are prevented from occurring.

**REFERENCES**

APPENDIX 1: ESTIMATION OF THE MODEL IMPULSE RESPONSES

To reduce the number of parameters to be estimated, each of the unknown impulse responses in Equation (1) was expanded as the sum of several weighted Meixner basis functions (MBF).

\[
h_{ABR}(t) = \sum_{j=0}^{q_{ABR}-1} c_{j}^{ABR} B_{j}^{(n)}(t) \quad (A1)
\]

\[
h_{RSA}(t) = \sum_{j=0}^{q_{RSA}-1} c_{j}^{RSA} B_{j}^{(n)}(t) \quad (A2)
\]

where the \( B_{j}^{(n)}(t) \) represents the \( j \)-th order discrete-time orthonormal Meixner function with \( n \)-th order of generalization which determines how late the MBF will start to fluctuate, and \( c_{j}^{ABR} \) and \( c_{j}^{RSA} \) are the corresponding unknown weights that are assigned to \( B_{j}^{(n)}(t) \) in the ABR and RSA impulse responses, respectively. Meixner basis functions (MBF) are a generalization of the discrete Laguerre basis functions (LBF). First, the LBF were generated. Then, the LBF were transformed to MBF. The \( j \)-th order MBF is defined as follows over the interval \( 0 \leq t \leq M-1 \):

\[
L_{0}(t) = \sqrt{v(t)} \quad (A3a)
\]

and

\[
L_{j}(t) = \sqrt{v(t)} L_{j-1}(t) + \sqrt{v(t)} L_{j-1}(t) - L_{j-1}(t-1), \quad 0 \leq j \leq q_{ABR} - q_{RSA} \quad (A3b)
\]

\( q_{ABR} \) and \( q_{RSA} \) represent the total number of Laguerre functions used in the expansion of the ABR and RSA impulse responses, respectively. In Equations (A3a) and (A3b), the parameter \( \alpha \) (\( 0 < \alpha < 1 \)) determines the rate of exponential decline of the Laguerre functions, and is selected such that, for given \( M, q_{ABR} \) and \( q_{RSA} \), the values of the constructed impulse response become insignificant as \( t \) approaches \( M \). The orthogonal matrix that transforms the LBF to the MBF can be expressed as

\[
A^{(n)} = X^{(n)}Y^{(n)} (A4)
\]

and \( X^{(n)} \) is an inversion of the Cholesky factorization of \( Y^{(n)} \).

Substituting Equations (A1) and (A2) into Equation (2), we obtain, after some algebraic manipulation:

\[
\Delta RRI(t) = \sum_{j=0}^{q_{ABR}-1} c_{j}^{ABR} u_{j}(t) + \sum_{j=0}^{q_{RSA}-1} c_{j}^{RSA} v_{j}(t) + \epsilon_{RRI}(t) \quad (A6)
\]

where \( u(t) \) and \( v(t) \) are new derived variables, defined as follows:

\[
u_{j}(t) = \sum_{i=0}^{M-1} B_{j}^{(n)}(i) \Delta V(t-i-\tau_{RSA}) \quad (A7)
\]

\[
v_{j}(t) = \sum_{i=0}^{M-1} B_{j}^{(n)}(i) \Delta SBP(t-i-\tau_{RSA}) \quad (A8)
\]

Equation (A6) becomes the new linear relation with unknown parameters \( c_{j}^{RSA} \) (\( 0 \leq j \leq q_{RSA} \)) and \( c_{j}^{ABR} \) (\( 0 \leq j \leq q_{ABR} \)) that can be estimated using least-squares minimization. However, note that Equation (A6) contains far fewer unknown parameters \( q_{RSA} + q_{ABR} \leq 2M \) than Equation (1).

First, the least-squares minimization procedure described...
above was repeated for a range of values for the delays ($\tau_{ABR}$ and $\tau_{RSA}$), the order of generalization ($n$ from 0 to 5), and Meixner function orders ($q_{ABR}$ and $q_{RSA}$ from 4 to 8). For each combination of delays, the order of generalization, and Meixner function orders, a metric of the quality of fit, known as the “minimum description length” (MDL), was computed. MDL was computed as follows:

$$\text{MDL} = \log(J_r) + \frac{\text{total number of parameters} \times \log(M)}{M} \quad (A9)$$

where $J_r$ is the variance of the residual errors between the measured data and the predicted output. Note that $\text{MDL}$ decreases as $J_r$ decreases but increases with increasing model order. Selection of the “optimal” candidate model was based on a global search for the minimum $MDL$; in addition, this “optimal” solution had to satisfy the condition that the cross-correlations between the residual errors and past values of the two inputs ($\Delta V(t)$ and $\Delta SBP(t)$) were statistically indistinguishable from zero. Once the optimal parameter values were determined, the ABR and RSA impulse responses were computed using Equations (A1) and (A2).

Finally, the recursive least squares (RLS) algorithm was used to estimate the autoregressive model coefficients at each time step. Basically, by using the RLS algorithm, the model coefficients were estimated by minimizing the residual, sum of squared error between the model prediction and the data. To make the results less sensitive to the remote past, the squared error between the model prediction and the data ($e$) was weighted as follows

$$J_w = \sum_{i=0}^{\text{lag}} \lambda^i e^2(t-i) \quad (A10)$$

where $\lambda$ is a forgetting factor and $0<\lambda<1$. The optimum $\lambda$ allows an RLS algorithm that has the fastest convergence and the most robustness.

The RLS algorithm was applied to each data set multiples time for $\lambda$ from 0.88 to 0.98. The $\lambda$ that minimized the mean square error between the model prediction and the data was selected.

**APPENDIX 2: TABLE OF ABBREVIATIONS**

<table>
<thead>
<tr>
<th>Symbol/Abbreviation</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABR</td>
<td>Baroreflex component of the model</td>
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<tr>
<td>BP</td>
<td>Blood pressure (arterial)</td>
</tr>
<tr>
<td>(\Delta RRI(t))</td>
<td>Fluctuation in RRI about the mean level at time $t$</td>
</tr>
<tr>
<td>(\Delta SBP(t))</td>
<td>Fluctuation in SBP about the mean level at time $t$</td>
</tr>
<tr>
<td>(\Delta V(t))</td>
<td>Change in incremental lung volume about the mean at time $t$</td>
</tr>
<tr>
<td>DBP</td>
<td>Diastolic blood pressure</td>
</tr>
<tr>
<td>(h_{ABR}(t))</td>
<td>Impulse response function of the ABR component</td>
</tr>
<tr>
<td>(h_{RSA}(t))</td>
<td>Impulse response function of the RSA component</td>
</tr>
<tr>
<td>HRV</td>
<td>Heart rate variability</td>
</tr>
<tr>
<td>(LFP_{DBP})</td>
<td>Low-frequency power of diastolic blood pressure variability</td>
</tr>
<tr>
<td>LHR</td>
<td>Ratio of low-frequency power to high-frequency power of RRI variability</td>
</tr>
<tr>
<td>RRI</td>
<td>R-R interval</td>
</tr>
<tr>
<td>RSA</td>
<td>Respiratory sinus arrhythmia component of model</td>
</tr>
<tr>
<td>SBP</td>
<td>Systolic blood pressure</td>
</tr>
<tr>
<td>(\tau_{ABR})</td>
<td>Latency associated with the baroreflex (ABR) component of the model</td>
</tr>
<tr>
<td>(\tau_{RSA})</td>
<td>Latency associated with the RSA component of the model</td>
</tr>
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